

**Bergen County Math League**

**Calculators Permitted**

**Good Luck to You**



**Good Luck to All**

**Contest #3**

**2024-2025 12 minutes**

**Questions 1 & 2**

- 3-1. In a contest, a total of \$1500 was given away in \$1, \$7, \$49, and \$343 prizes. No prize was awarded more than six times. How many \$1 prizes were given away in this contest?
- 3-2. In  $\triangle ABC$ ,  $m\angle A = 45$  and  $m\angle B > m\angle C$ . The length of the altitude from  $B$  is 6, and the perimeter of the triangle is  $24 + 6\sqrt{2}$ . Find the area of  $\triangle ABC$ .

**Bergen County Math League**

**Calculators Permitted**

**Good Luck to You**



**Good Luck to All**

**Contest #3**

**2024-2025 12 minutes**

**Questions 3 & 4**

- 3-3. If  $5x^3 + 3x^2 - 4x + 7 = a + b(x - 1) + c(x - 1)^2 + d(x - 1)^3$  is an identity for all real values of  $x$ , find the value of  $a$ .
- 3-4. Find the radius-length of the circle whose area is tripled when the length of its radius is increased by 2.

**Bergen County Math League  
Calculators Permitted**

**Good Luck to You**



**Good Luck to All**

**Contest #3**

**2024-2025 12 minutes**

**Questions 5 & 6**

- 3-5. The function  $f$ , defined on the positive integers, satisfies

$$f(n) + f(n + 1) = 11 - n$$

for all integral values of  $n$  from 1 through 8 inclusive. If

$$f(9) + f(1) = 2,$$

find the value of  $f(1)$ .

- 3-6. Arcs  $ABC$  and  $ADC$  are different semicircles of the same circle of which  $\overline{AB}$  and  $\overline{AD}$  are chords. Further,  $AB = 2$  and  $AD = 5$ . From points  $B$  and  $D$ , perpendiculars are drawn to  $\overline{AC}$ , intersecting  $\overline{AC}$  at points  $E$  and  $F$  respectively. If  $AE = x$ ,  $EF = 3$ , and  $FC = y$ , find the sum  $x + y$ .